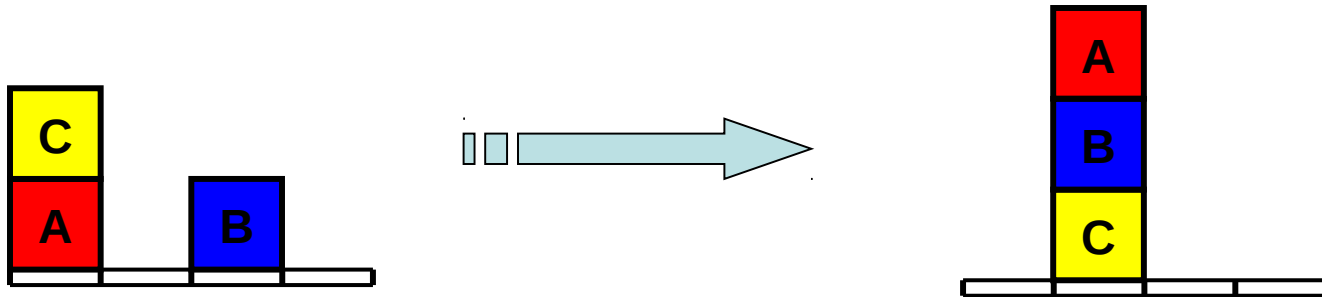


# Planning Problems

---

Want a sequence of actions to turn a start state into a goal state

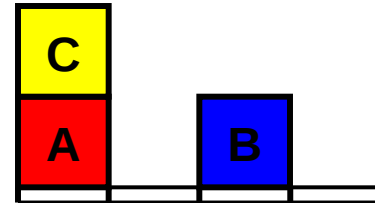


Unlike generic search, states and actions have internal structure, which allows better search methods

# State Space

---

|              |
|--------------|
| On(C, A)     |
| On(A, Table) |
| On(B, Table) |
| Clear(C)     |
| Clear(B)     |



## Representation

States described by propositions or ground predicates

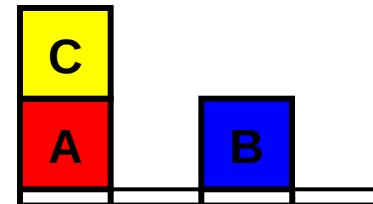
Sparse encoding (database semantics): all unstated literals are false

Unique names: each object has its own single symbol

# Actions

---

On(C, A)  
On(A, Table)  
On(B, Table)  
Clear(C)  
Clear(B)



ACTION: Move(b,x,y)

PRECONDITIONS: On(b,x), Clear(b), Clear(y)

POSTCONDITIONS: On(b,y), Clear(x)

$\neg$ On(b,x),  $\neg$ Clear(y)

ACTION: Move(C,A,Table)

PRECONDITIONS: On(C,A), Clear(C), Clear(Table)

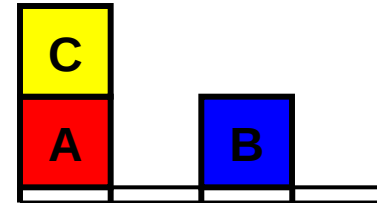
POSTCONDITIONS: On(C,Table), Clear(A)

$\neg$ On(C,A),  $\neg$ Clear(Table)

# Actions

---

On(C, A)  
On(A, Table)  
On(B, Table)  
Clear(C)  
Clear(B)



ACTION: MoveToBlock(b,x,y)

PRECONDITIONS: On(b,x), Clear(b), Clear(y),  
Block(b), Block(y), (b≠x), (b≠y), (x≠y)

POSTCONDITIONS: On(b,y), Clear(x)  
¬On(b,x), ¬Clear(y)

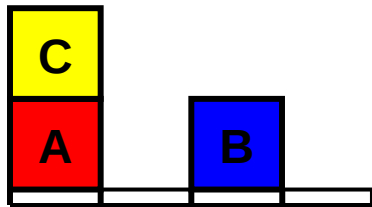
ACTION: MoveToTable(b,x)

PRECONDITIONS: On(b,x), Clear(b), Block(b), Block(x), (b≠x)

POSTCONDITIONS: On(b,Table), Clear(x)  
¬On(b,x)

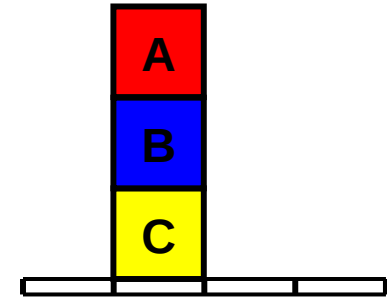
# Start and Goal States

---



Start State

On(C, A)  
On(A, Table)  
On(B, Table)  
Clear(C)  
Clear(B)  
Block(A)  
...



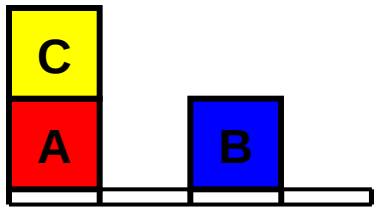
Goal State

On(B, C)  
On(A, B)

Important: goal  
satisfied by any  
state which  
entails goal list

[MoveToTable(C,A), Move(B,Table,C), Move(A,Table,B)]

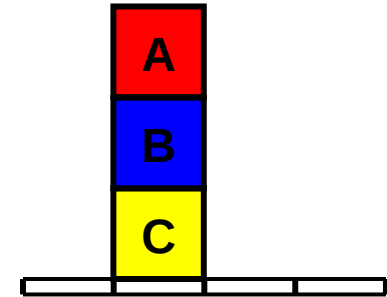
# Planning Problems



On(C, A)  
On(A, Table)  
On(B, Table)  
Clear(C)  
Clear(B)

Sparse encoding,  
but complete  
state spec

Action schema,  
instantiates to give  
specific ground actions



Goal

Set of goal states,  
only requirements  
specified (think  
unary constraints)

On(B, C)  
On(A, B)

**Which goal first?**

ACTION: MoveToTable(b,x)

PRECONDITIONS: On(b,x), Clear(b), Block(b), Block(x), (b≠x)

POSTCONDITIONS: On(b,Table), Clear(x)

$\neg$ On(b,x)

# Practice

---

Problem 10.2: “Applicable”

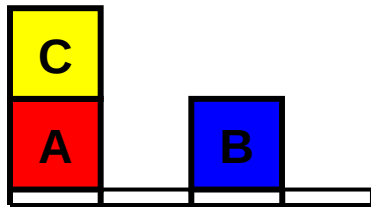
Problem 10.3a,b: Representation

Where do they come from?

Could they be learned?

# Kinds of Plans

---



Start State

On(C, A)  
On(A, Table)  
On(B, Table)  
Clear(C)  
Clear(B)  
Block(A)  
...

## Sequential Plan

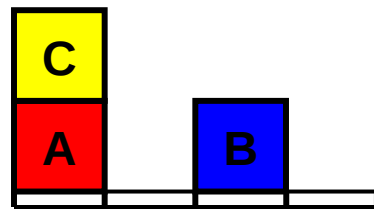
MoveToTable(C,A) > Move(B,Table,C) > Move(A,Table,B)

## Partial-Order Plan

MoveToTable(C,A)  
Move(B,Table,C) > Move(A,Table,B)]



# Forward Search



Start State

On(C, A)  
On(A, Table)  
On(B, Table)  
Clear(C)  
Clear(B)  
Block(A)  
...

MoveToTable(C,A)

MoveToBlock(C,A,B)

MoveToBlock(B, Table, C)

~~On(C, A)~~  
On(A, Table)  
On(B, Table)  
Clear(C)  
Clear(B)  
Block(A)  
...  
+Clear(A)  
+On(C, Table)

Applicable actions

# Backward Search

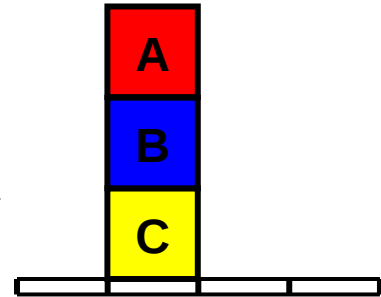
ACTION: MoveToBlock(b,x,y)  
PRECONDITIONS: On(b,x), Clear(b), Clear(y),  
Block(b), Block(y), (b≠x), (b≠y),  
(x≠y)  
POSTCONDITIONS: On(b,y), Clear(x)  
¬On(b,x), ¬Clear(y)

MoveToBlock(A, Table, B)

MoveToBlock(A, x', B)

On(B, C)  
~~On(A, B)~~  
+On(A, Table)  
+Clear(A)  
+Clear(B)  
+...

Relevant actions



Goal State

On(B, C)  
On(A, B)

$$g' = (g - \text{ADD}(a)) \cup \text{Precond}(a)$$



# Heuristics: Ignore Preconditions

Relax problem by ignoring preconditions

Can drop all or just some preconditions

Can solve in closed form or with set-cover methods

|   |   |   |
|---|---|---|
| 7 | 2 | 4 |
| 5 |   | 6 |
| 8 | 3 | 1 |

Start State

|   |   |   |
|---|---|---|
|   | 1 | 2 |
| 3 | 4 | 5 |
| 6 | 7 | 8 |

Goal State

$Action(Slide(t, s_1, s_2),$

PRECOND:  $On(t, s_1) \wedge Tile(t) \wedge Blank(s_2) \wedge Adjacent(s_1, s_2)$

EFFECT:  $On(t, s_2) \wedge Blank(s_1) \wedge \neg On(t, s_1) \wedge \neg Blank(s_2)$

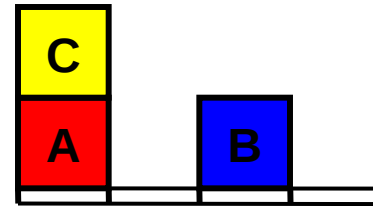
# Heuristics: No-Delete

---

Relax problem by not deleting falsified literals

Can't undo progress, so solve with hill-climbing (non-admissible)

|              |
|--------------|
| On(C, A)     |
| On(A, Table) |
| On(B, Table) |
| Clear(C)     |
| Clear(B)     |



ACTION: MoveToBlock(b,x,y)

PRECONDITIONS: On(b,x), Clear(b), Clear(y),  
Block(b), Block(y), (b≠x), (b≠y), (x≠y)

POSTCONDITIONS: On(b,y), Clear(x)  
¬On(b,x), ¬Clear(y)

# Heuristics: Independent Goals

---

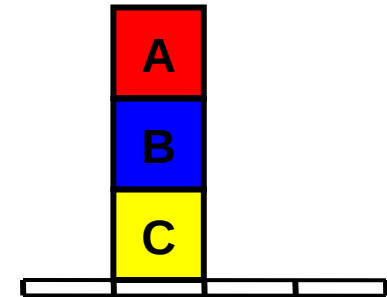
## Independent subgoals?

Partition goal literals

Find plans for each subset

$\text{cost}(\text{all}) < \text{cost}(\text{any})?$

$\text{cost}(\text{all}) < \text{sum-cost}(\text{each})?$



Goal State

On(B, C)  
On(A, B)

On(A, B)

On(B, C)



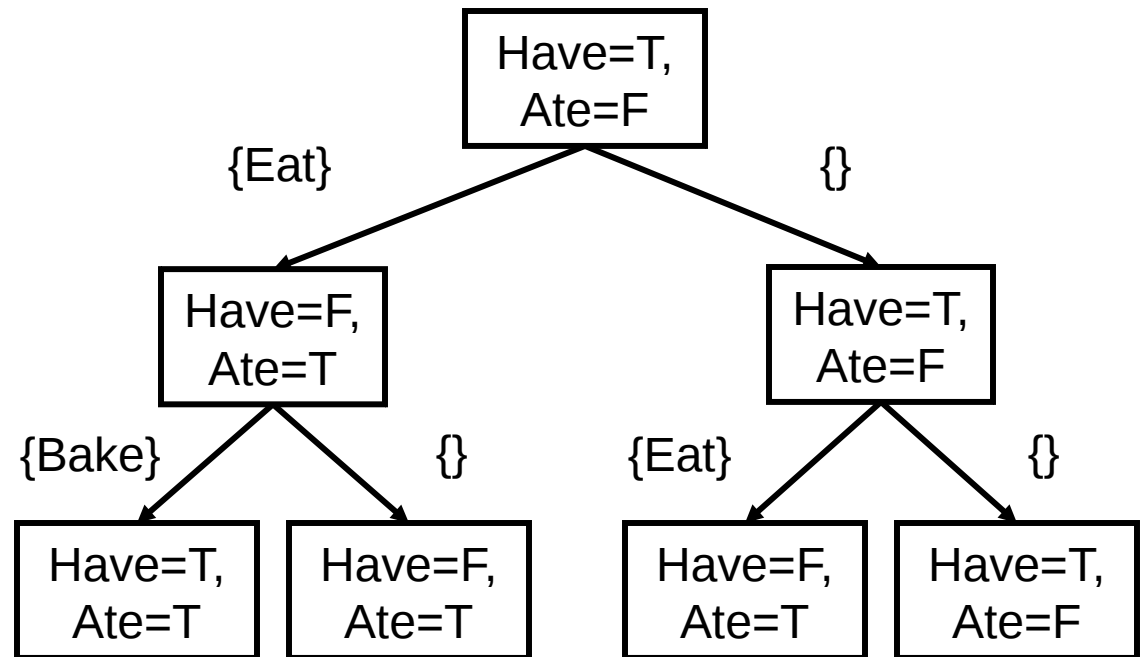
# Planning “Tree”

Start: HaveCake

Goal: AteCake, HaveCake

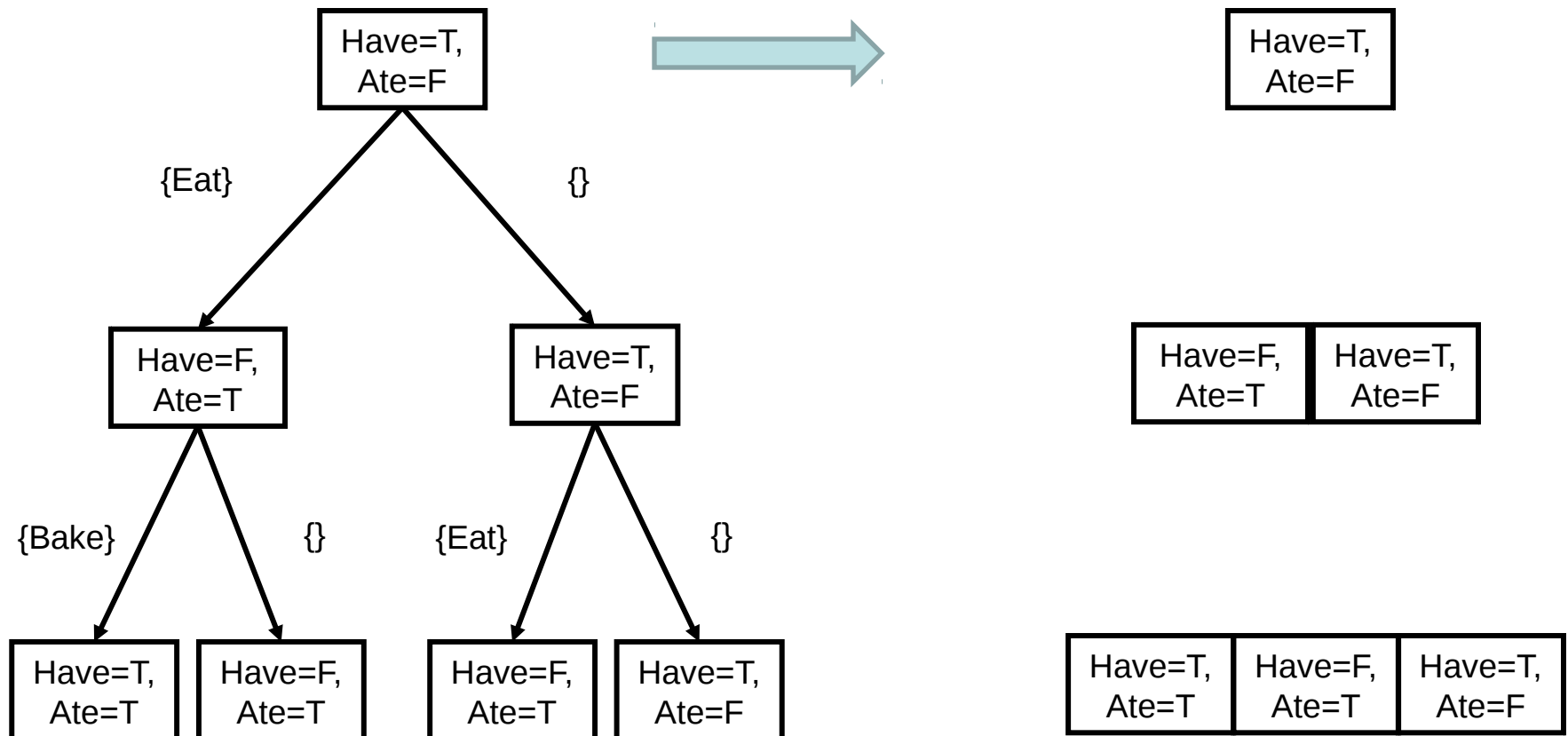
Action: Eat  
Pre: HaveCake  
Add: AteCake  
Del: HaveCake

Action: Bake  
Pre:  $\neg$ HaveCake  
Add: HaveCake





# Reachable State Sets



# Approximate Reachable Sets

---

Have=T,  
Ate=F



Have={T},  
Ate={F}

|                  |                  |
|------------------|------------------|
| Have=F,<br>Ate=T | Have=T,<br>Ate=F |
|------------------|------------------|

Have={T,F},  
Ate={T,F}

(Have, Ate) not (T,T)  
(Have, Ate) not (F,F)

|                  |                  |                  |
|------------------|------------------|------------------|
| Have=T,<br>Ate=T | Have=F,<br>Ate=T | Have=T,<br>Ate=F |
|------------------|------------------|------------------|

Have={T,F},  
Ate={T,F}

(Have,Ate) not (F,F)

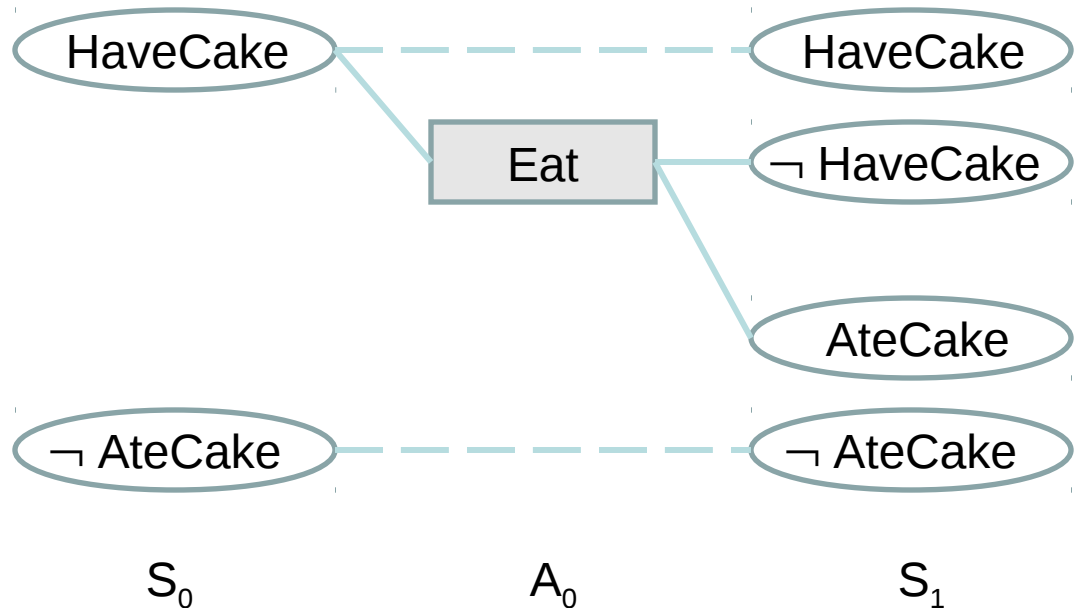
# Planning Graphs

Start: HaveCake

Goal: AteCake, HaveCake

Action: Eat  
Pre: HaveCake  
Add: AteCake  
Del: HaveCake

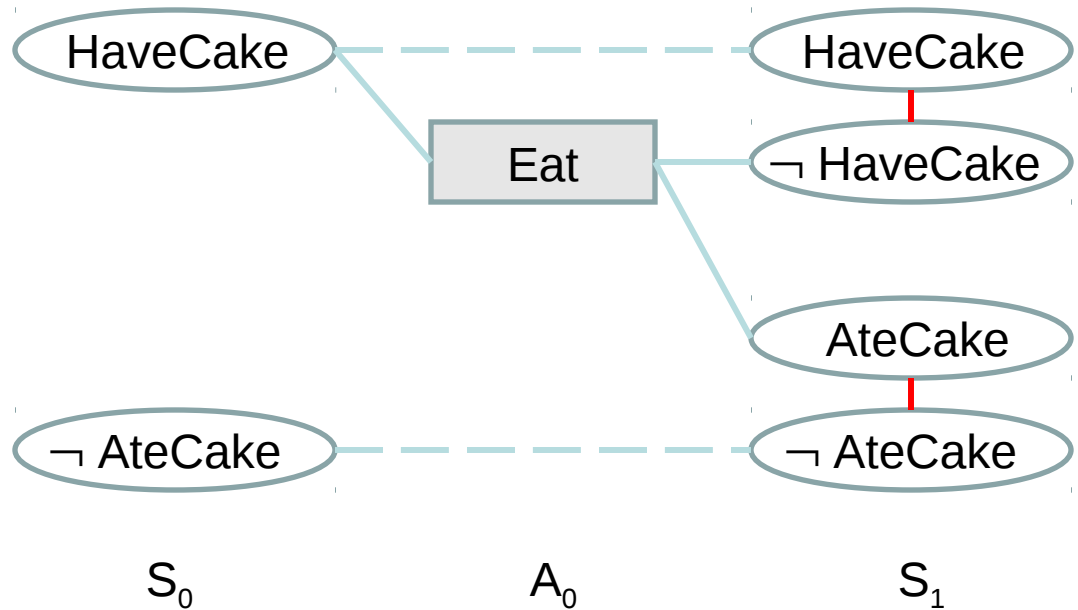
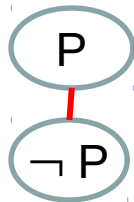
Action: Bake  
Pre:  $\neg$ HaveCake  
Add: HaveCake



# Mutual Exclusion (Mutex)

## NEGATION

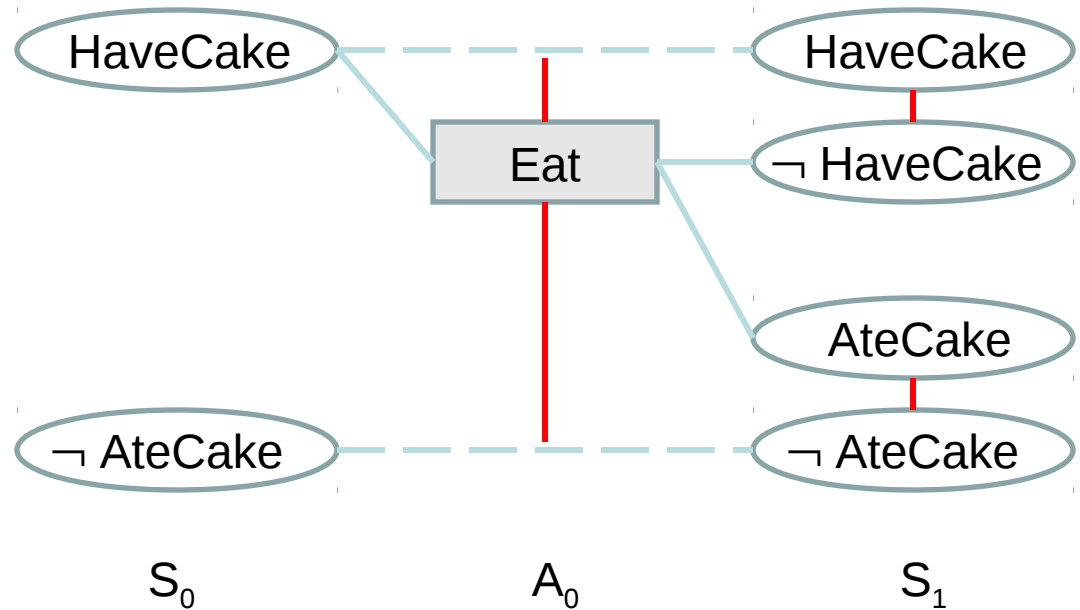
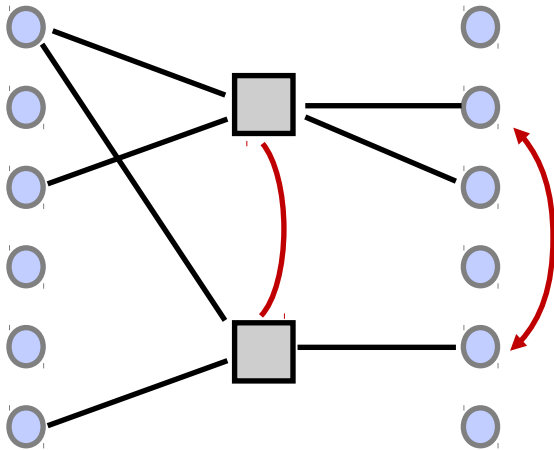
*Literals and their negations can't be true at the same time*



# Mutual Exclusion (Mutex)

## *INCONSISTENT EFFECTS*

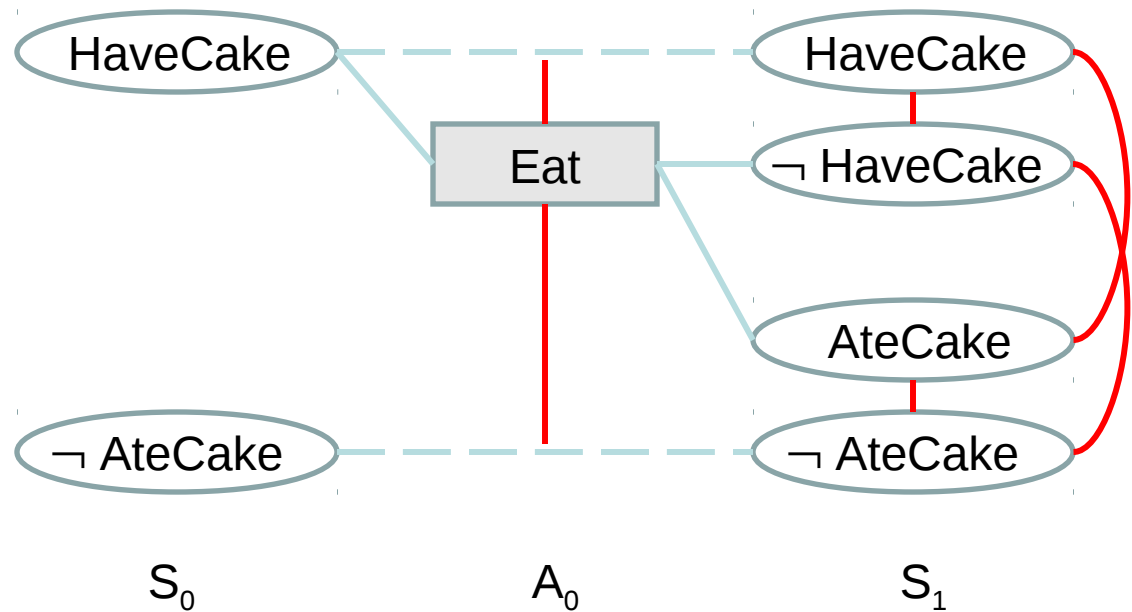
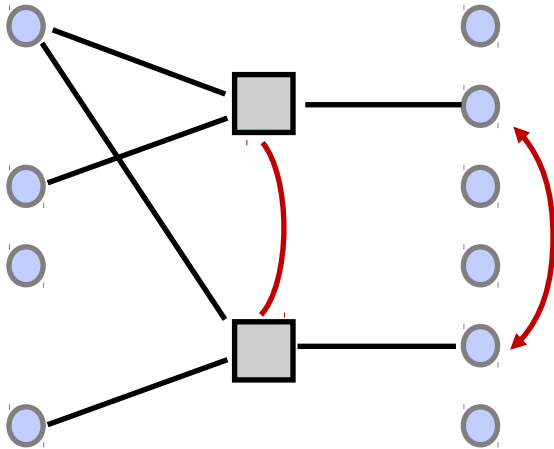
*An effect of one  
negates the  
effect of the other*



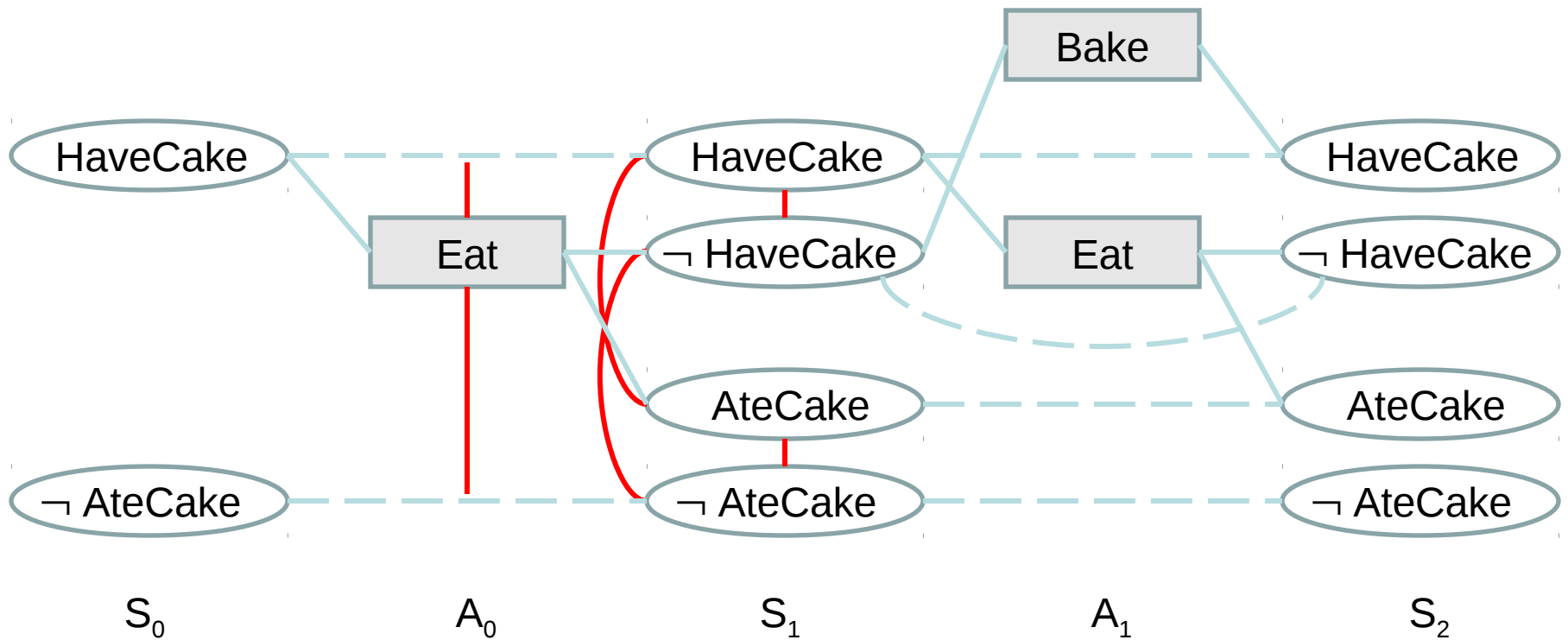
# Mutual Exclusion (Mutex)

## *INCONSISTENT SUPPORT*

*All pairs of actions  
that achieve two  
literals are mutex*



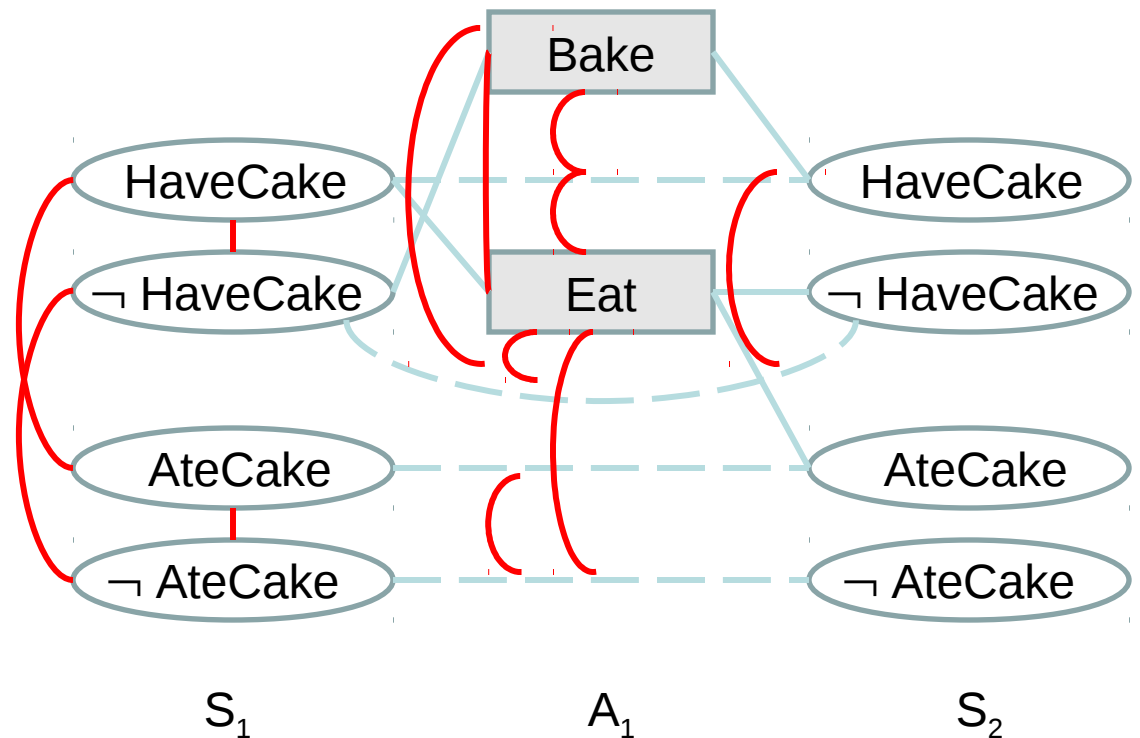
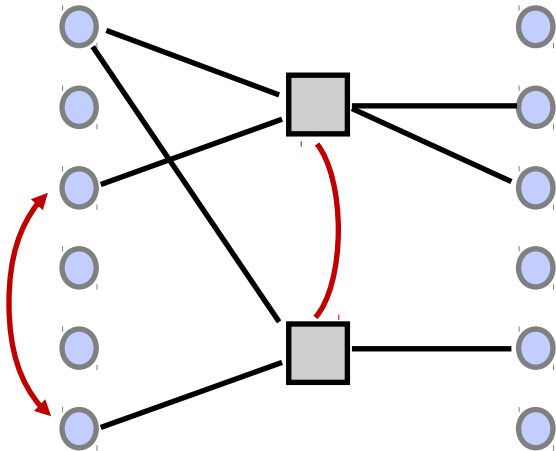
# Planning Graph



# Mutual Exclusion (Mutex)

## COMPETITION

Preconditions are mutex; cannot both hold



## INCONSISTENT EFFECTS

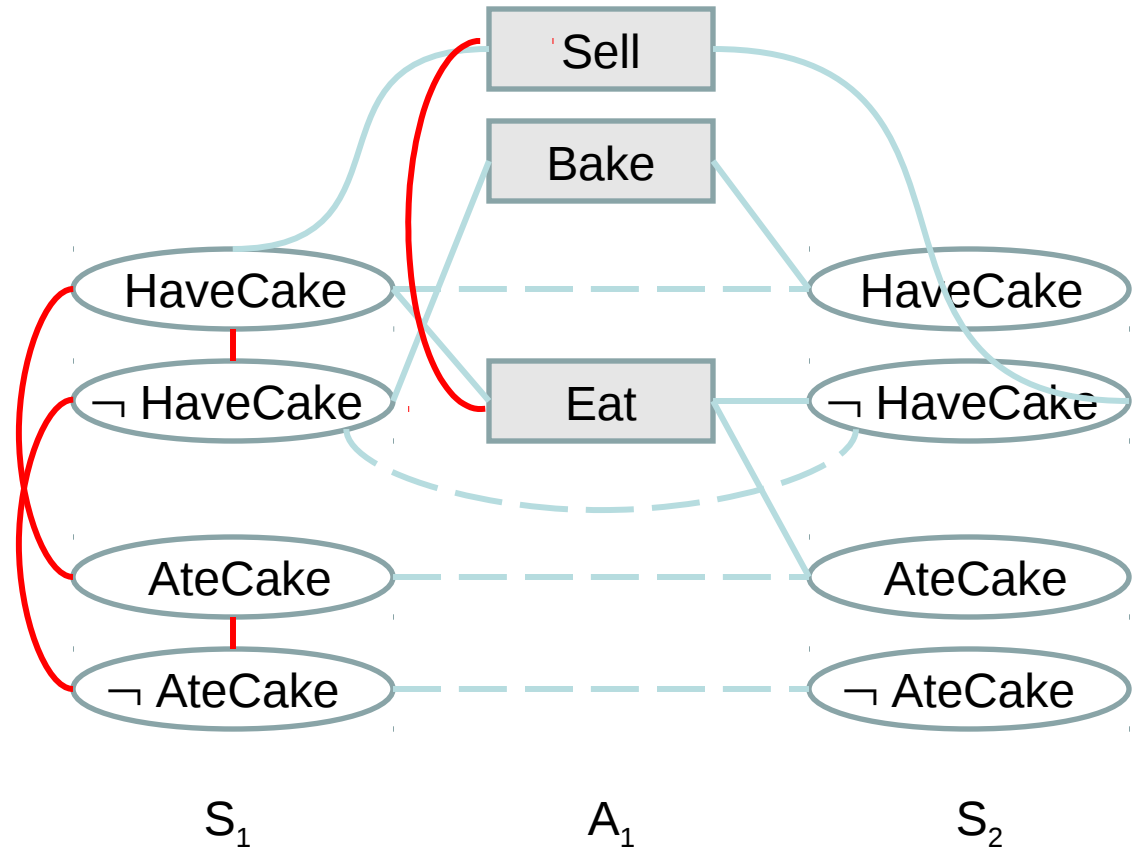
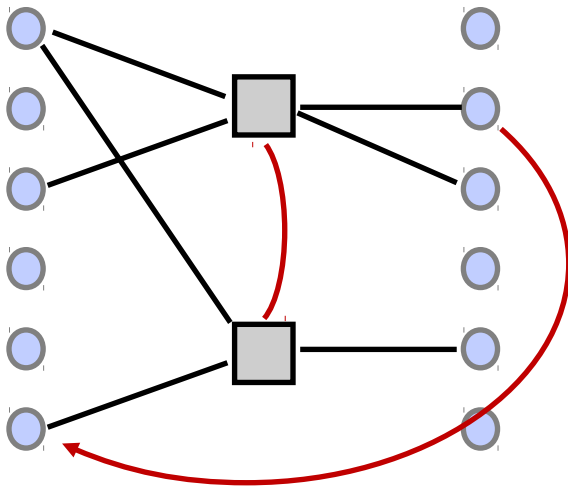
An effect of one negates the effect of the other



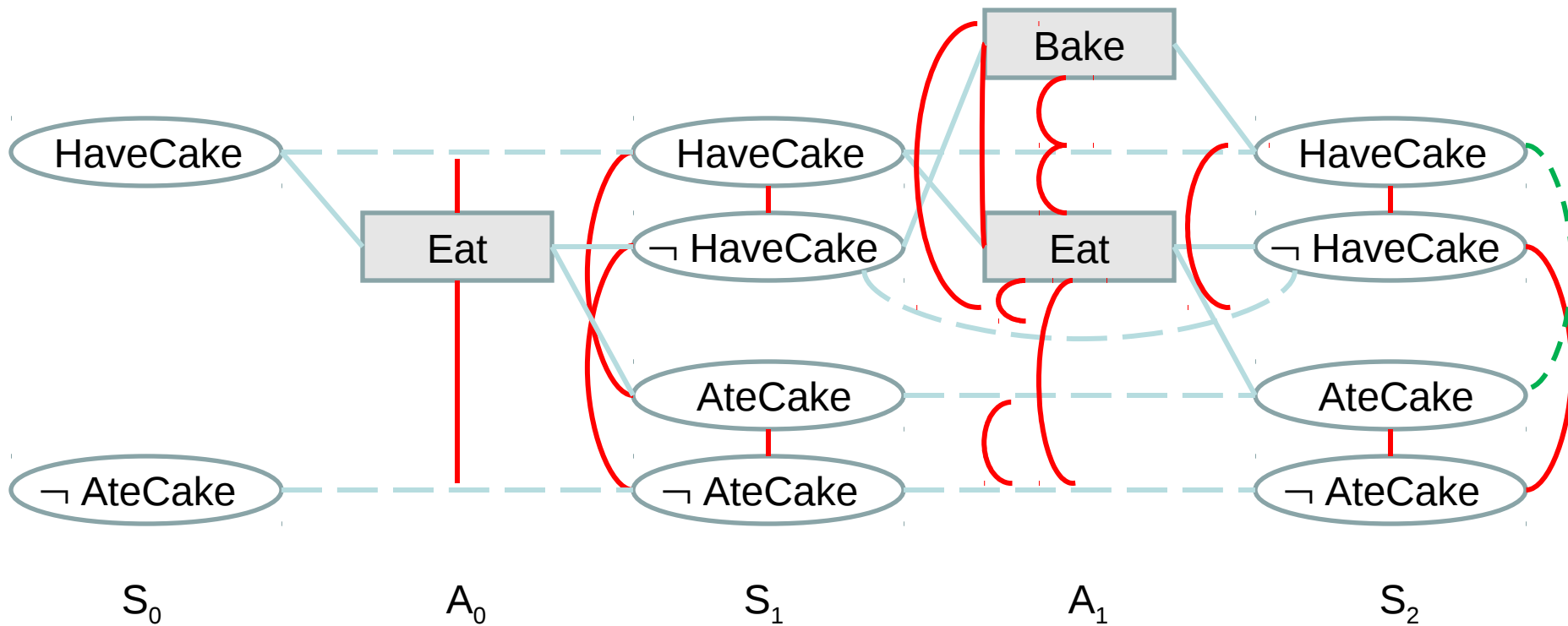
# Mutual Exclusion (Mutex)

## *INTERFERENCE*

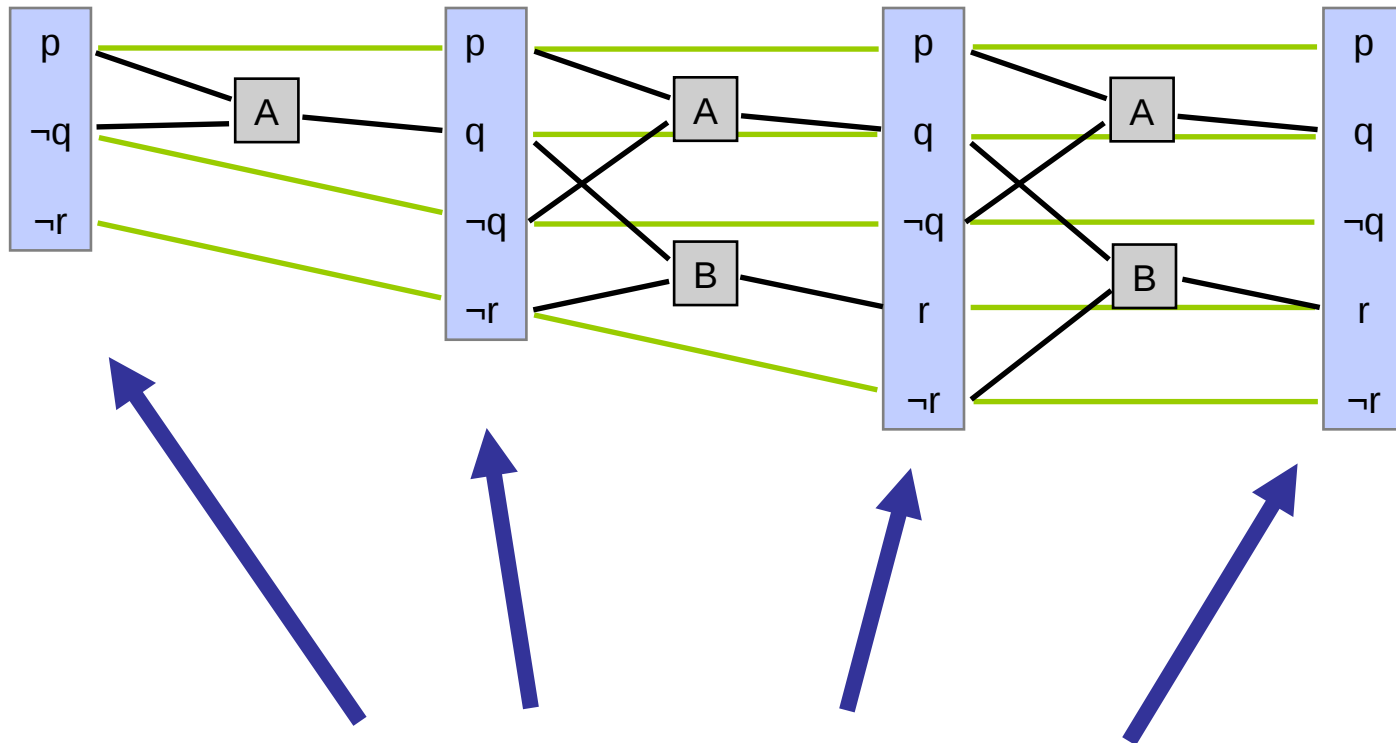
*One deletes a precondition of the other*



# Planning Graph

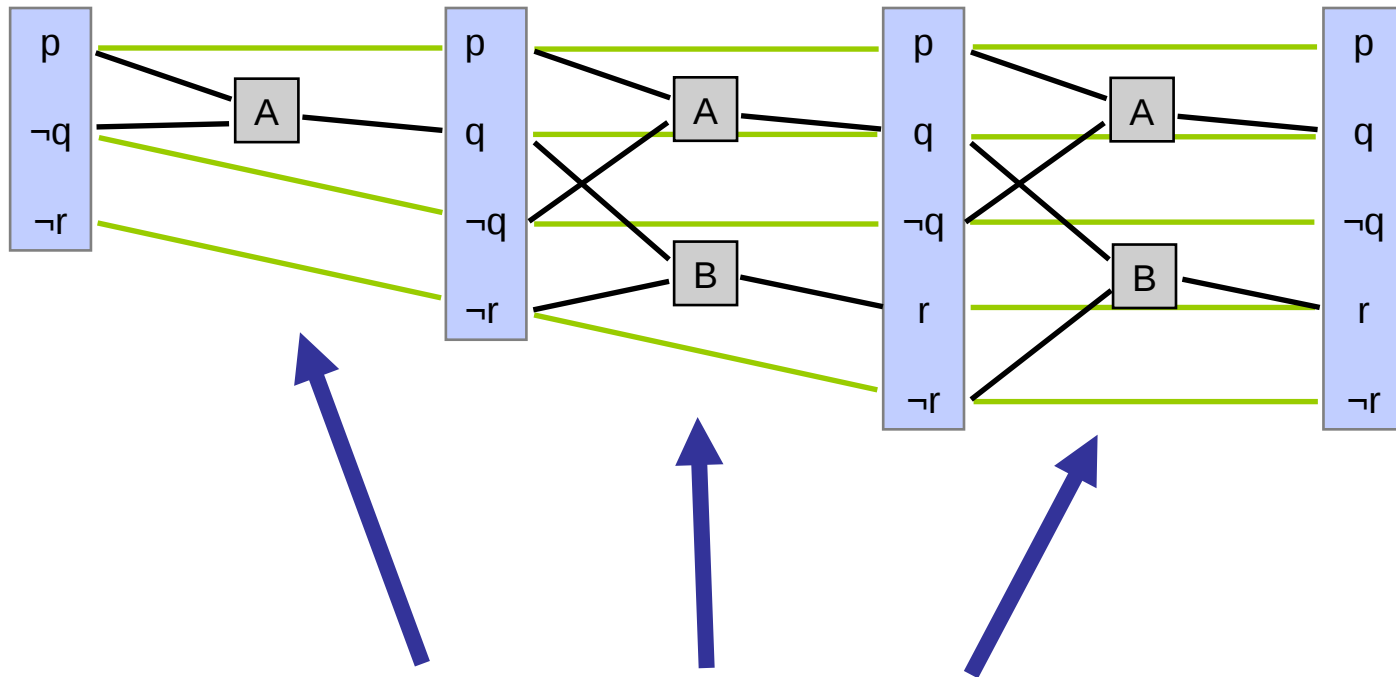


# Observation 1



Propositions monotonically increase  
(always carried forward by no-ops)

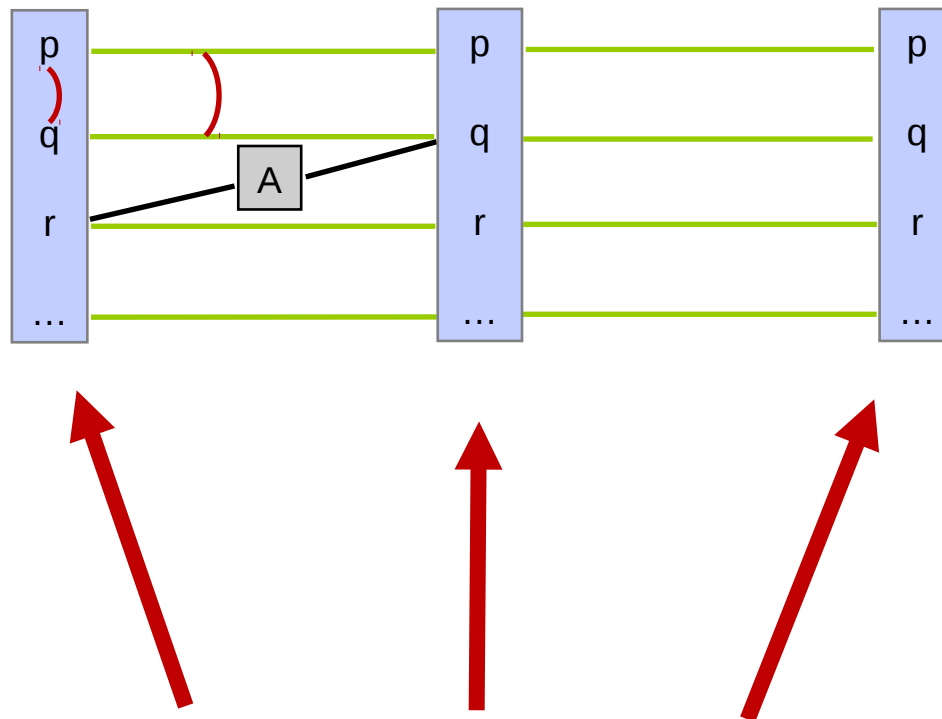
# Observation 2



Actions monotonically increase  
(if they applied before, they still do)

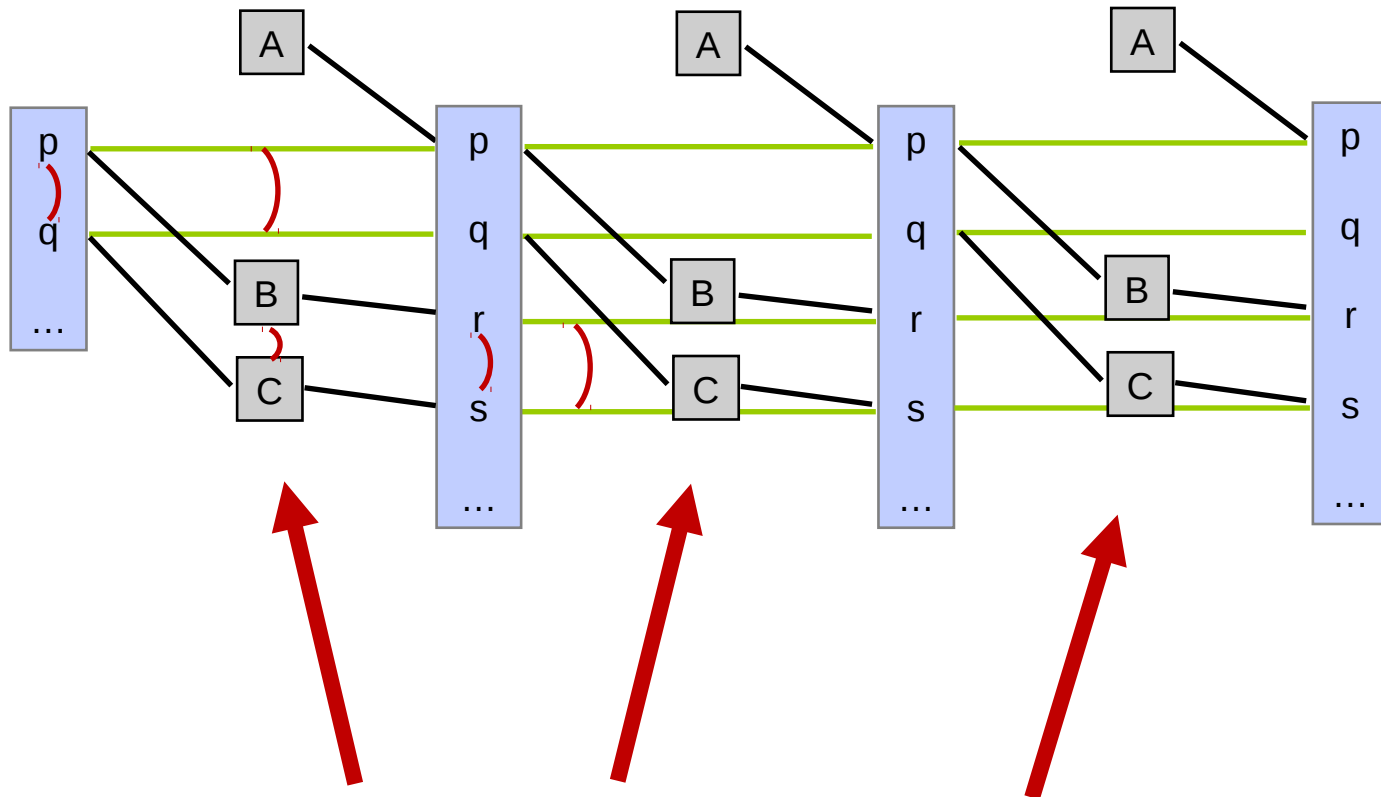
# Observation 3

---



Proposition mutex relationships monotonically decrease

# Observation 4



Action mutex relationships monotonically decrease

# Observation 5

---

Claim: planning graph “levels off”

After some time  $k$  all levels are identical

Because it's a finite space, the set of literals cannot increase indefinitely, nor can the mutexes decrease indefinitely

Claim: if goal literal never appears, or goal literals never become non-mutex, no plan exists

If a plan existed, it would eventually achieve all goal literals (and remove goal mutexes – less obvious)

Converse not true: goal literals all appearing non-mutex does not imply a plan exists

# Heuristics: Level Costs

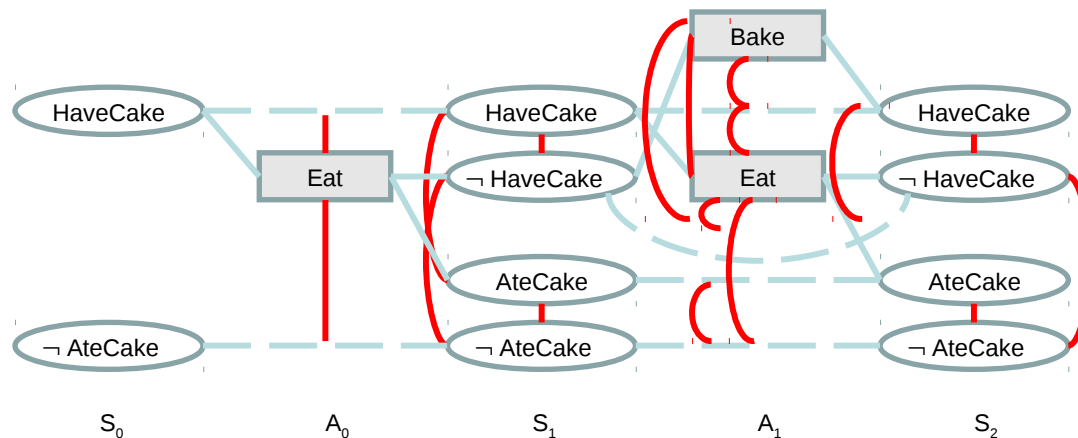
## Planning graphs enable powerful heuristics

Level cost of a literal is the smallest  $S$  in which it appears

Max-level: goal cannot be realized before largest goal conjunct level cost (admissible)

Sum-level: if subgoals are independent, goal cannot be realized faster than the sum of goal conjunct level costs (not admissible)

Set-level: goal cannot be realized before all conjuncts are non-mutex (admissible)





# Graphplan

---

Graphplan directly extracts plans from a planning graph

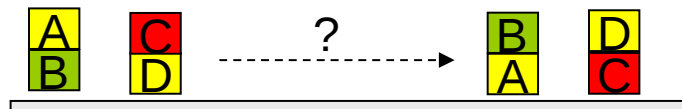
Graphplan searches for **layered plans** (often called parallel plans)

More general than totally-ordered plans, less general than partially-ordered plans

A layered plan is a sequence of **sets** of actions

actions in the same set must be compatible

all sequential orderings of compatible actions gives same result



**Layered Plan:** (a two layer plan)

$$\left\{ \begin{array}{l} \text{move(A,B,TABLE)} \\ \text{move(C,D,TABLE)} \end{array} \right\} \cdot \left\{ \begin{array}{l} \text{move(B,TABLE,A)} \\ \text{move(D,TABLE,C)} \end{array} \right\}$$

# Solution Extraction: Backward Search

## Search problem:

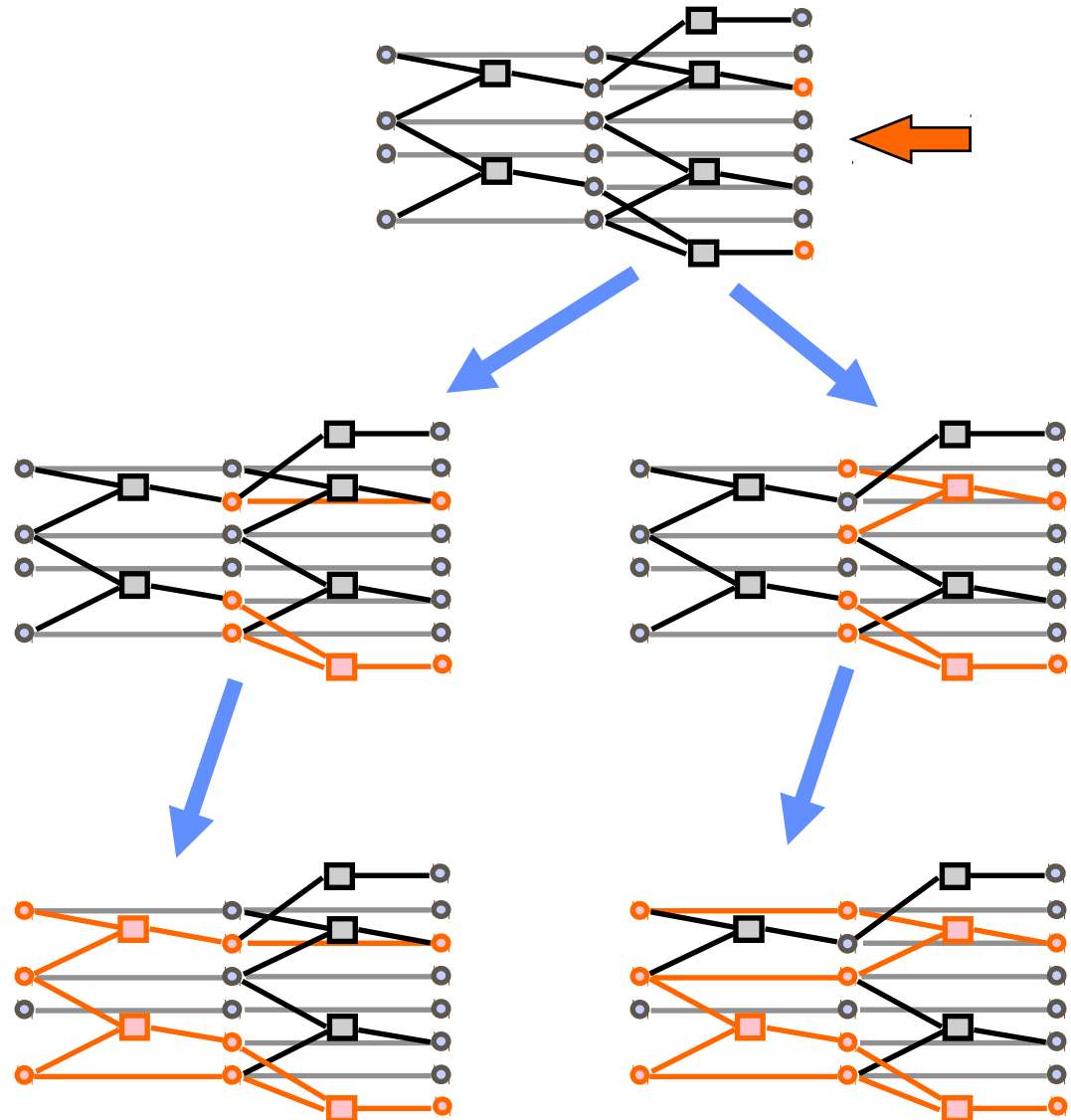
Start state: goal set at last level

Actions: conflict-free ways of achieving the current goal set

Terminal test: at  $S_0$  with goal set entailed by initial planning state

Note: may need to start much deeper than the leveling-off point!

Caching, good ordering is important





# Scheduling

---

In real planning problems, actions take time, resources

Actions have a duration (time to completion, e.g. building)

Actions can consume (or produce) resources (or both)

Resources generally limited (e.g. minerals, SCVs)

Simple case: known (partial) plan, just need to schedule

Even simpler: no resources, just ordering and duration

## JOBS

[AddEngine1 < AddWheels1 < Inspect1]

[AddEngine2 < AddWheels2 < Inspect2]

## RESOURCES

EngineHoists (1)

WheelStations (1)

Inspectors (2)

## ACTIONS

AddEngine1: DUR=30, USE=EngHoist(1)

AddEngine2: DUR=60, USE=EngHoist(1)

AddWheels1: DUR=30, USE=WStation(1)

AddWheels2: DUR=15, USE=WStation(1)

Inspect1: DUR=10, USE=Inspectors(1)

Inspect2: DUR=10, USE=Inspectors(1)

# Resource-Free Scheduling

## JOBS

[AddEngine1 < AddWheels1 < Inspect1]  
[AddEngine2 < AddWheels2 < Inspect2]

## RESOURCES

EngineHoists (1)  
WheelStations (1)  
Inspectors (2)

## ACTIONS

AddEngine1: DUR=30, USE=EngHoist(1)  
AddEngine2: DUR=60, USE=EngHoist(1)  
AddWheels1: DUR=30, USE=WStation(1)  
AddWheels2: DUR=15, USE=WStation(1)  
Inspect1: DUR=10, USE=Inspectors(1)  
Inspect2: DUR=10, USE=Inspectors(1)

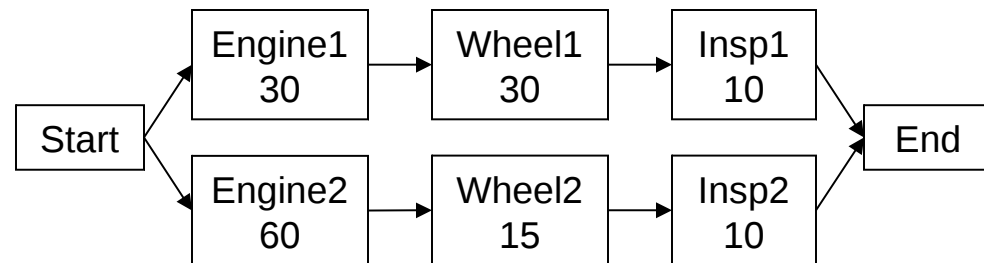
How to minimize total time?

Easy: schedule an action as soon as  
its parents are completed

$$ES(START) = 0$$

$$ES(a) = \max_{b: b \prec a} ES(b) + DUR(b)$$

Result:



# Resource-Free Scheduling

## JOBS

[AddEngine1 < AddWheels1 < Inspect1]  
[AddEngine2 < AddWheels2 < Inspect2]

## RESOURCES

EngineHoists (1)  
WheelStations (1)  
Inspectors (2)

## ACTIONS

AddEngine1: DUR=30, USE=EngHoist(1)  
AddEngine2: DUR=60, USE=EngHoist(1)  
AddWheels1: DUR=30, USE=WStation(1)  
AddWheels2: DUR=15, USE=WStation(1)  
Inspect1: DUR=10, USE=Inspectors(1)  
Inspect2: DUR=10, USE=Inspectors(1)

Note there is always a **critical path**

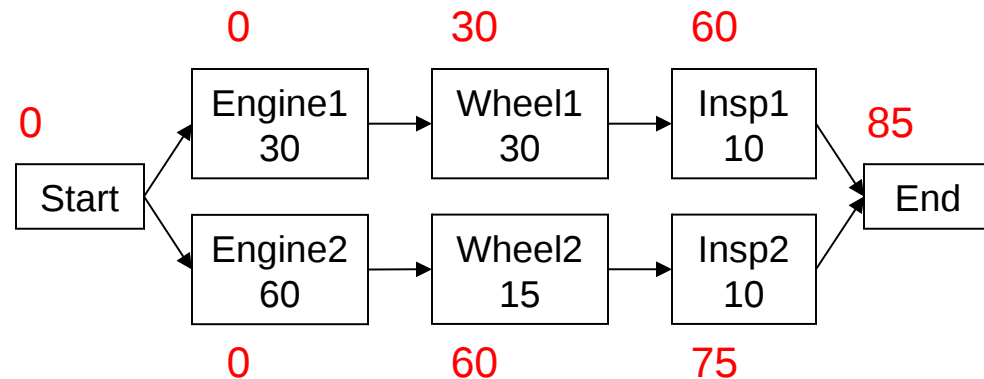
All other actions have **slack**

Can compute slack by computing  
latest start times

$$LS(END) = ES(END)$$

$$LS(a) = \min_{b:a \prec b} LS(b) - DUR(a)$$

Result:



# Adding Resources

For now: consider only released (non-consumed) resources

View start times as variables in a CSP

Before: conjunctive linear constraints

$$\forall b : b \prec a \quad ES(a) \geq ES(b) + DUR(b)$$

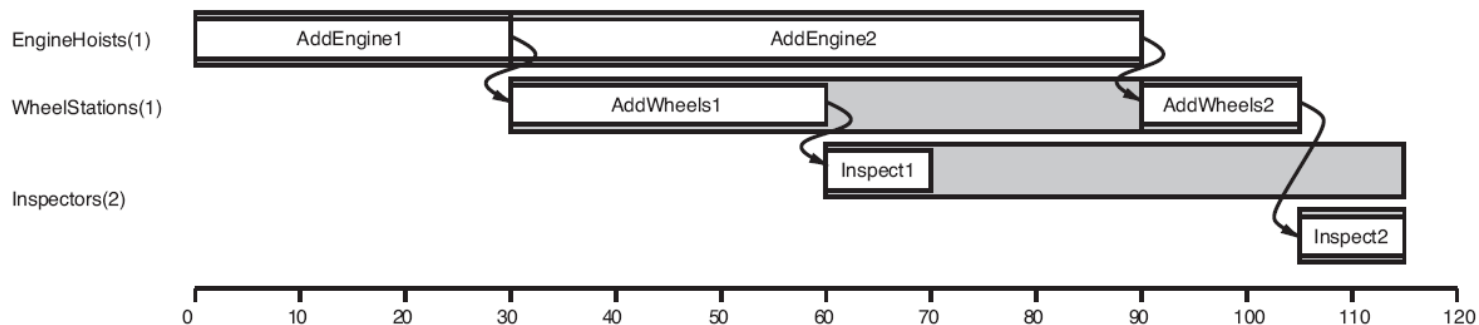
Now: disjunctive constraints (competition)

if competing( $a, b$ )

$$ES(a) \geq ES(b) + DUR(b) \vee$$

$$ES(b) \geq ES(a) + DUR(a)$$

In general, no efficient method for solving optimally



# Adding Resources

One greedy approach: min slack algorithm

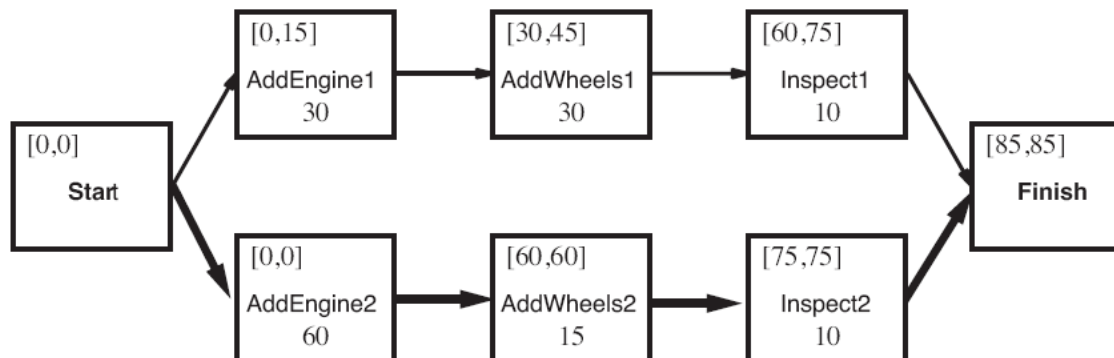
Compute ES, LS windows for all actions

Consider actions which have all preconditions scheduled

Pick the one with least slack

Schedule it as early as possible

Update ES, LS windows (recurrences now must avoid reservations)





# Resource Management

---

## Complications:

Some actions need to happen at certain times

Consumption and production of resources

Planning and scheduling generally interact